



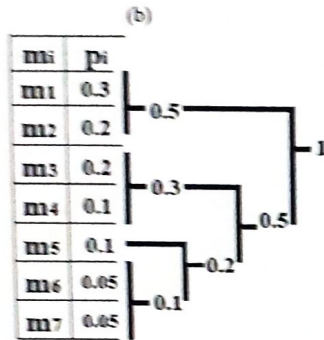
Information Coding and Security EXAM

Nom :
 Prénom : *Farid*

07^{pts.} Exercise 1: Consider the following codes:

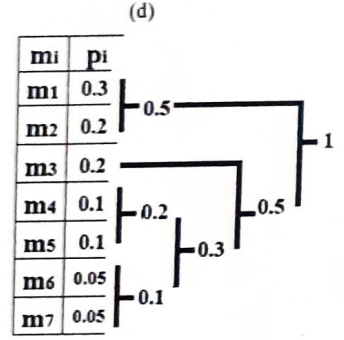
(a)

m_i	p_i	I	II	III	IV
m_1	0.3	1	1		
m_2	0.2	1	0		
m_3	0.2	0	1		
m_4	0.1	0	0	1	1
m_5	0.1	0	0	1	0
m_6	0.05	0	0	0	1
m_7	0.05	0	0	0	0



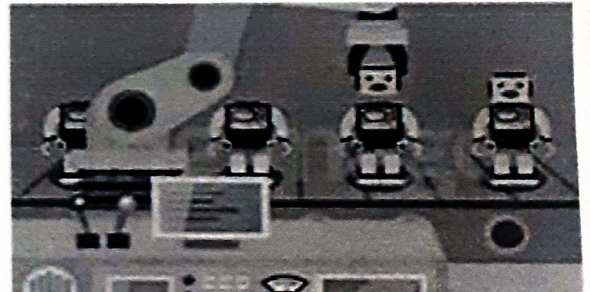
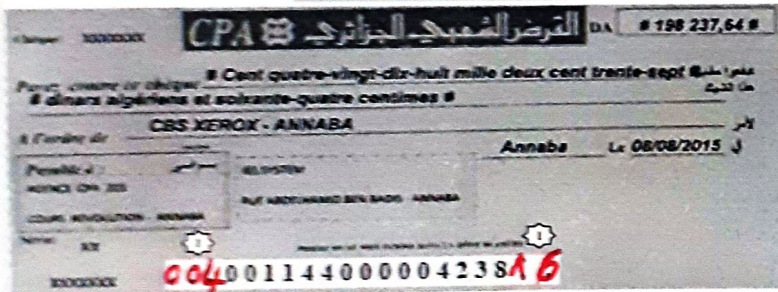
(c)

m_i	p_i	I	II	III	IV
m_1	0.3	1	1		
m_2	0.2	1	0		
m_3	0.2	0	1	1	
m_4	0.1	0	1	0	
m_5	0.1	0	0	1	
m_6	0.05	0	0	0	1
m_7	0.05	0	0	0	0



- ✓ The maximum of Entropy is : $\log_2 7 = \ln 7 / \ln 2 = 2.81 \text{ bit./mess}$
- ✓ The invalid code is : *a*
- ✓ The efficient Shannon Fano code is : *c*....., and it's variance is : $\sigma^2 = 0.44 \Rightarrow \sigma = 0.66$
- ✓ The efficient Huffman code is : *b*....., and it's average length is : $L_{avg} = 2.6 \text{ bits./mess}$
- ✓ The least efficient code is : *a*....., and it's variance is : $\sigma^2 = 0.84 \Rightarrow \sigma = 0.91$

07^{pts.} Exercise 2: Complete to create a valid code ?



06^{pts.} Exercise 3:

✓ Consider a Hamming code, and fill in the tables below?

Information : m_i	Code word : C_i
1 1 1 0	1 1 1 0 0 0 0
0 1 1 1	0 1 1 1 1 0 0
0 1 0 1	0 1 0 1 0 1 0
0 1 1 0	0 1 1 0 0 1 1
1 0 0 0	1 0 0 0 0 1 1
1 0 1 1	1 0 1 1 0 1 0

Received code word C_i	Corrected code word C_i
1 0 1 1 0 1 1	1 0 1 1 0 1 0
0 0 0 0 1 1 0	0 0 0 0 1 1 0
1 1 1 0 1 1 1	1 1 1 0 1 1 1
1 1 0 0 1 0 1	1 1 0 0 1 0 1
1 0 1 0 0 0 1	1 0 1 0 0 0 1
1 0 0 1 1 1 1	1 0 0 1 1 1 1



Information Coding and Security EXAM

Nom :
 Prénom : **B**

07 pts. Exercise 1: Consider the following codes:

mi	pi	I	II	III	IV
m1	0.3	1	1		
m2	0.2	1	0		
m3	0.2	0	1	1	
m4	0.1	0	1	0	
m5	0.1	0	0	1	
m6	0.05	0	0	0	1
m7	0.05	0	0	0	0

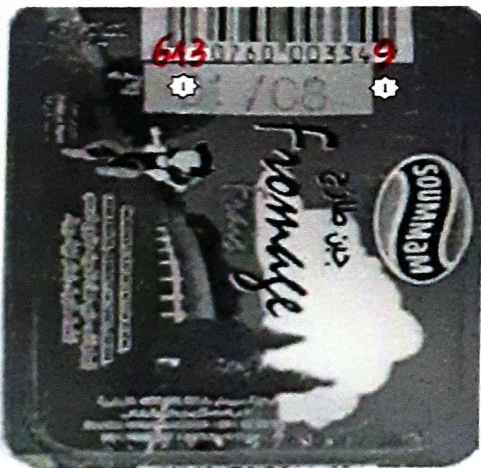
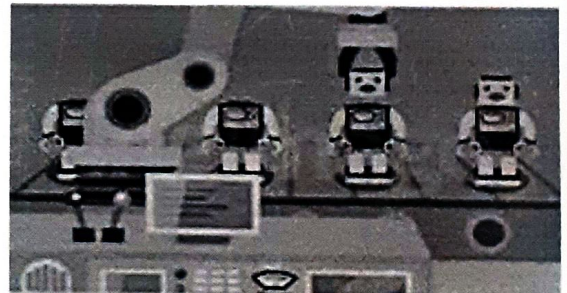
mi	pi
m1	0.3
m2	0.2
m3	0.2
m4	0.1
m5	0.1
m6	0.05
m7	0.05

mi	pi	I	II	III	IV
m1	0.3	1	1		
m2	0.2	1	0		
m3	0.2	0	1		
m4	0.1	0	0	1	1
m5	0.1	0	0	1	0
m6	0.05	0	0	0	1
m7	0.05	0	0	0	0

mi	pi
m1	0.3
m2	0.2
m3	0.2
m4	0.1
m5	0.1
m6	0.05
m7	0.05

- ✓ The maximum of Entropy is : $H = \log_2 7 = 2.81 \text{ bit/mess}$
- ✓ The invalid code is : **b**
- ✓ The efficient Shannon Fano code is : **a**, and its variance is : $\sigma^2 = 0.44 \Rightarrow \sigma = 0.66$
- ✓ The efficient Huffman code is : **d**, and its average length is : $L_{av} = 2.6 \text{ bit/mess}$
- ✓ The least efficient code is : **c**, and its variance is : $\sigma^2 = 0.84 \Rightarrow \sigma = 0.91$

07 pts. Exercise 2: Complete to create a valid code ?



06 pts. Exercise 3:

✓ Consider a Hamming code, and fill in the tables below?

Information : mi	Code word : Ci
0 1 0 1	0 1 0 1 0 1 0
0 1 1 0	0 1 1 0 0 1 1
1 1 1 0	1 1 1 0 0 0 0
0 1 1 1	0 1 1 1 1 0 0
1 0 0 0	1 0 0 0 0 1 1
1 0 1 1	1 0 1 1 0 1 0

Received code word Ci	Corrected code word Ci
1 1 1 0 1 1 1	1 1 1 0 1 1 1
1 1 0 0 1 0 1	0 1 0 0 1 0 1
1 0 1 1 1 0 1	1 0 1 1 0 1 0
0 0 0 0 1 1 0	0 0 1 0 1 1 0
1 0 1 0 0 0 1	1 0 1 0 0 0 1
1 0 0 1 1 1 1	0 0 0 1 1 1 1