

Module: Fundamental Electrical Engineering 1

L2 ST

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Exam (1h :30 min)

.....: اللقب

.....: الاسم

.....: الشعبة : الفوج

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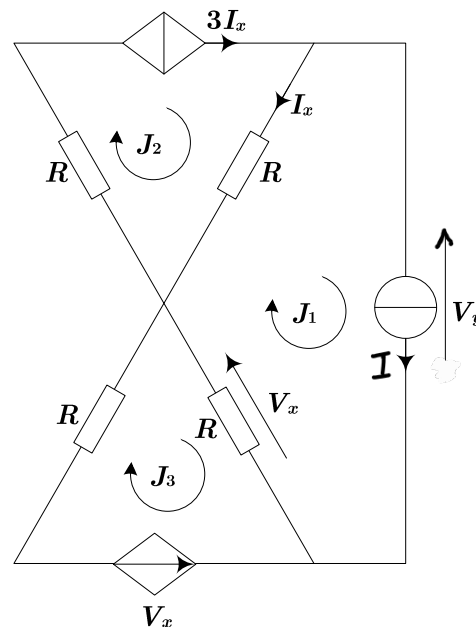
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Exercise 1 (6 pts)

Using the mesh analysis, find J_1 , J_2 and J_3 .

Deduce the voltage V_y .

$I = 12 \text{ A}$, $R = 10 \Omega$.



Solution

Mesh (1): 0.75 pt

..... $J_1 = I$

Mesh (2): $J_2 = 3I_x$ 0.75 pt

Mesh (3): $V_x + R J_3 + R (J_3 - J_1) = 0$ 0.75 pt

$I_x = J_2 - J_1$ $V_x = R (J_3 - J_1)$ $V_y = R (J_1 - J_2) + R (J_3 - J_2)$

0.5 pt

0.5 pt

0.75 pt

0.5 pt

0.5 pt

0.5 pt

0.5 pt

$J_1 = \dots 12 \dots \text{ A}$

$J_2 = \dots 18 \dots \text{ A}$

$J_3 = \dots 8 \dots \text{ A}$

$V_y = \dots 20 \dots \text{ V}$

Exercise 2 (2 pts)

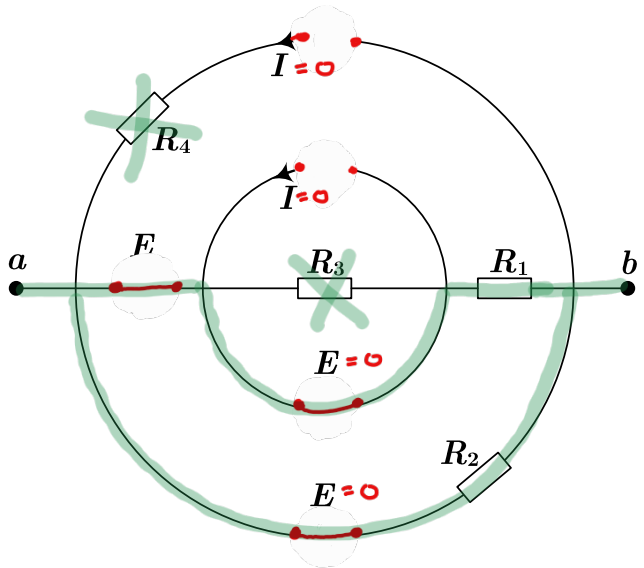
Find the Thevenin's resistor between *a* and *b*.

$R_1=10\Omega, R_2=15, R_3=20\Omega, R_4=15\Omega.$

Solution

$R_{Th} = \dots \frac{R_1 // R_2}{R_1 + R_2} \dots$ 1 pt

$R_{Th} = \dots 6 \dots \Omega$ 1 pt



Exercise 3 (6 pts)

Using the nodal analysis, find V_1, V_2 and V_3 .

Deduce the voltage V_y .

$E = 120V, I = 10A, R = 10\Omega.$

Solution

Node (1,2): 0.75 pt

(S.N.): $\frac{V_2}{R} + \frac{V_2 - V_3}{R} = I - I_x$

Node (1,2): $V_1 - V_2 = V_x$ 0.75 pt

Node (3): $V_3 = E$ 0.75 pt

$I_x = \dots \frac{-V_2}{R} \dots$ $V_x = \dots V_3 - V_2 \dots$ $V_y = \dots V_1 + RI \dots$

0.5 pt

0.5 pt

0.75 pt

0.5 pt

0.5 pt

0.5 pt

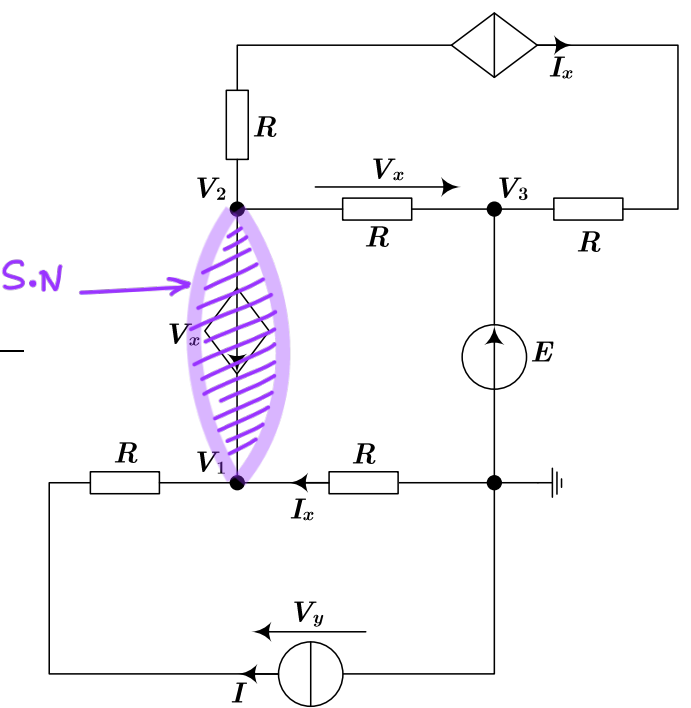
0.5 pt

$V_1 = \dots 120 \dots V$

$V_2 = \dots 220 \dots V$

$V_3 = \dots 120 \dots V$

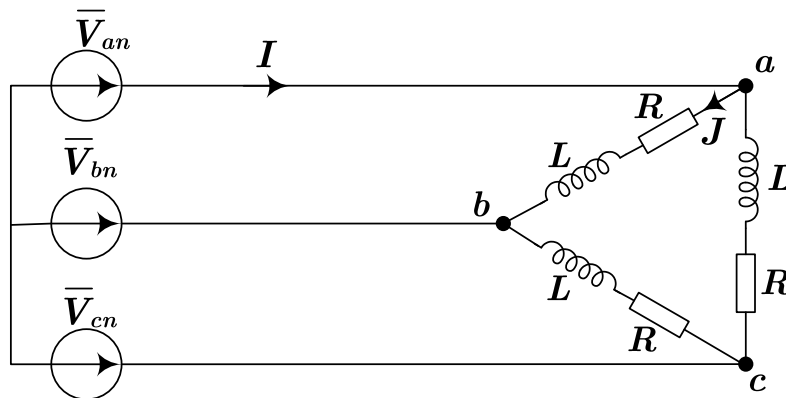
$V_y = \dots 220 \dots V$



Exercise 3 (6 pts)

The three-phase balanced system 220/380V 50Hz in the figure below supplies a three inductive impedances $\bar{Z} = 50\angle 45^\circ \Omega$ contains $R=?$, $L=100\text{ mH}$.

- 1- What is the type of connection?
- 2- What the voltage across each impedance.
- 3- Calculate the value of the resistance R .
- 4- Calculate the phase current J , the line current I , and the power factor.
- 5- Calculate the active power P , reactive Q , and apparent power S .
- 6- Calculate the capacitor coupled in delta that raises the power factor to 1.
- 7- In the phasor diagram showing below, represent the vectors : U_{ab} , U_{bc} , U_{ca} , J_{ab} , J_{bc} , J_{ca} .



Solution

1- The type of connection is : *Delta* 0.25 pt

2- The voltage across each impedance is *380* V 0.25 pt

3- Calculation of resistance R :

$$R = \sqrt{Z^2 - (L\omega)^2} \dots\dots\dots R = \boxed{38.9} \Omega$$

380 / 50

4- Calculation of the phase current J , line current I , and the power factor PF .

$$J = \frac{U}{Z} \dots\dots\dots J = \boxed{7.6} A, \quad I = \sqrt{3}J \dots\dots\dots I = \boxed{13.16} A, \quad PF = \cos(45^\circ) \dots\dots\dots PF = \boxed{0.7}$$

5- Powers calculation

• $P = \sqrt{3} U \cdot I \cdot \cos \varphi$ $P = 6.12 \text{ kW}$

0.25 pt

0.25 pt

• $Q = \sqrt{3} U \cdot I \sin \varphi$ $Q = 6.12 \text{ kVar}$

0.25 pt

0.25 pt

• $S = \sqrt{3} U \cdot I = \sqrt{P^2 + Q^2}$ $S = 7.24 \text{ kVA}$

0.25 pt

0.25 pt

6- Capacitor calculation

• $C = \frac{P (\tan(45^\circ) - \tan(0^\circ))}{3 U^2 \cdot \omega}$ $C = 4.50 \times 10^{-5} \text{ F}$

0.25 pt

0.25 pt

7- Phasor diagram, Representation of the vectors: U_{ab} , U_{bc} , U_{ca} , J_{ab} , J_{bc} , J_{ca}

